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THEORETICAL CONCEPTS & APPLICATIONS OF INDEPENDENT COMPONENT ANALYSIS

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Abstract- This paper deals with the study of Independent Component Analysis. Independent Component Analysis is basically a method which is used to implement the concept of Blind Source Separation. Blind Source Separation is a technique which is used to extract set of source signal from set of their mixed source signals. The various techniques which are used for implementing Blind Source Separation totally depends upon the properties and the characteristics of original sources. Also there are many fields nowadays in which Independent Component Analysis is widely used. This paper deals with the theoretical concepts of Independent Component Analysis, its principles and its widely used applications.

Keywords- Independent Component Analysis, Blind Source Separation, Scatter Plot, Decorrelation, Non-Gaussian.

I. INTRODUCTION

Independent Component Analysis (ICA) is one of the major technique used to implement Blind Source Separation. As the various methods used for BSS basically distinguished on the basis of some peculiar properties of original sources or the input sources, so the basic property which we used for ICA is statistical independence between the sources. Uncorrelatedness and non-gaussianity between the sources are also used for developing the algorithm the ICA.

II. THEORETICAL CONCEPT OF ICA

Independent Component Analysis is a computational method of separating a multivariate signal into additive sub components supposing mutual statistical independence of the source Signals. Here independent components means that all the observed signal should be statistically independent, i.e. no component of one signal must be related to any component of other signal. ICA is a special case of blind source separation. The most important concept which is used to implement ICA is the property of statistical independence which must be present between the original sources. By using this technique a linear transformation of original independent sources is observed. Independent Component Analysis can be divided into noiseless and noisy case. Noiseless ICA can be considered as a special case of noisy ICA.

III. STATISTICAL INDEPENDENCE

In probability theory two events are said to be statistically independent if the probability of occurrence of one event does not affect the probability of occurrence of other event. In the similar way we can say for random variables that the two random variables are independent if the occurrence of one event does not affect the probability distribution of other event. Condition of statistical independence for two events Two events A and B are independent if and only if their joint probability equals the product of their probabilities:

\[ P(A \cap B) = P(A)P(B) \]

IV. DEFINITION OF ICA

“We have given a set of observations of random variables \( x_1(t), x_2(t) \ldots x_n(t) \), where \( t \) is the time or
The theoretical concepts and applications of Independent Component Analysis (ICA) are discussed in this document. The focus is on understanding how signals can be separated into their independent components, even when they are mixed together. The document explains how ICA algorithms estimate both the mixing matrix and the independent components from observed signals.

## V. ICA MODELS

### Linear Noiseless ICA

The components $x_i$ of the observed random vector are generated as a sum of the independent components:

$$x_i = a_{i1}s_1 + \ldots + a_{ik}s_k + \ldots + a_{in}s_n$$  \hspace{1cm} (1)

where $a_{ij}$ are coefficients that depend on the distance between speaker and microphone. The sources $S$ can be recovered by multiplying the observed signals $X$ with the inverse of the mixing matrix $W=A^{-1}$, known as the unmixing matrix.

### Linear Noisy ICA

With the added assumption of zero-mean and uncorrelated Gaussian noise, the ICA model takes the form:

$$X = A*S + n$$ \hspace{1cm} (4)

## VI. DEMONSTRATION OF ICA

We have been given a set of observations of random variables $(x_1(t), x_2(t), \ldots)$ where $t$ is the time or sample index. Now assume that they are generated as a linear mixture of independent components. The components are non-Gaussian. The basic concept of non-Gaussianity can be implemented with the help of the Central Limit Theorem, which states that the sum of non-Gaussian random variables is closer to Gaussian in comparison with the original individual ones.

## VII. PRINCIPLE

ICA basically works on two principles:

**Principle 1: Uncorrelatedness**
- This is one of the important assumptions which explain the first principle of ICA. This principle states that if we want to recover original independent signals, there will be some restriction on input sources, such that they are uncorrelated to each other.

**Principle 2: Maximum Non-Gaussianity**
- The second principle of ICA states that to get our original sources, there is one more restriction on the input sources, such that they must be non-Gaussian.

## VIII. CONCEPT OF SCATTER PLOT

To check the precise results at the output, we can make use of a scatter plot or scatter diagram. A scatter diagram is a tool for analysing relationships between two variables. One variable is plotted on the horizontal axis, and the other is plotted on the vertical axis. The pattern of their intersecting points can graphically show relationship patterns. Most often a scatter diagram is used to prove or disprove cause-and-effect relationships.

While the diagram shows relationships, it does not by itself prove that one variable causes the other. In addition to showing possible cause-and-effect relationships, a scatter diagram can show that two variables are from a common cause that is unknown or that one variable can be used as a surrogate for the other. We can use scatter plots for various purposes to examine theories about cause-and-effect relationships and to search for root causes of an identified problem. Scatter diagrams will generally show one of six possible correlations.

- **Strong Positive Correlation**: The value of $Y$ clearly increases as the value of $X$ increases.
Fig 4: Scatterplot showing strong positive correlation

- Strong Negative Correlation: The value of Y clearly decreases as the value of X increases.

Fig 5: Scatterplot showing weak positive correlation

- Weak Positive Correlation: The value of Y increases lightly as the value of X increases.

Fig 6: Scatterplot showing strong negative correlation

- Weak Negative Correlation: The value of Y decreases slightly as the value of X increases.

Fig 7: Scatterplot showing weak negative correlation

- Complex Correlation: The value of Y seems to be related to the value of X, but the relationship is not easily determined.

Fig 8: Scatterplot showing complex correlation

- No-Correlation: There is no demonstrated connection between the two variables.

Fig 9: Scatterplot showing no correlation

IX. APPLICATIONS OF ICA

- Cocktail Party Problem
  The Cocktail Party Effect also known as selective attention is the phenomenon of being able to focus one’s auditory attention on a particular stimulus while filtering out a range of other stimuli. The Cocktail Party Problem is illustrated in Fig.9. If each of the J voices you can hear at a party is recorded by N microphones, the recordings will be a matrix composed of a set of N vectors, each of

Fig 10: Diagram showing concept of Cocktail party problem

which is a (weighted) linear superposition of the J voices. For a discrete set of M samples, we can denote the sources by an J ×M matrix, Z, and the N recordings by an N × M matrix X. Z is therefore transformed into the observables X (through the propagation of sound waves through the room) by multiplying it by a N × J mixing matrix A such that $X = AZ$. Figure.(10) illustrates this paradigm where sound waves from J = 3 independent speakers (z₁, z₂, and z₃, left) are superimposed (centre), and recorded as three mixed source vectors with slightly different phases and volumes at three spatially separated but otherwise identical microphones. In order for us to ‘pick out’ a voice from an ensemble of voices in a crowded room, we must perform some type of BSS to recover the original sources from the observed mixture. Mathematically, we want to find a demixing matrix W, which when multiplied by the Recordings Xᵀ, produces an estimate Yᵀ of the sources Zᵀ. Therefore W is a set of Weights (approximately 16) equal to A inverse. One of the key methods for performing BSS is known as ICA.[5]
• **ICA in CDMA communications**

Nowadays CDMA technique is widely used for communication purpose. As CDMA has more advantages as compared to FDMA and TDMA. CDMA systems require more advanced signal processing methods, and correct reception of CDMA signals is more difficult because of several disturbing phenomena. A serious problem is multipath propagation. In case of direct sequence CDMA data can be cast in form of linear ICA.

The transmitted symbols have a number of possible values, and the spreading code of the desired user is known. Also multipath propagation and time delays make separation of desired user symbol a challenging task for linear ICA. In the first stage of this project, we applied ICA and BSS methods to various problems in multiuser detection, trying to take into account the available prior information. In particular, we have considered estimation of the desired user's time delay, estimation of fading channels in , and detection of the desired user's symbol sequence . The results are very good showing that ICA based methods can yield better performances than more conventional methods.

In the second stage, independent component analysis is applied to blind suppression of interference caused by bit-pulsed jamming in a direct sequence CDMA communication system. This jamming problem is important in practical CDMA communication systems. We have taken into account both data modulation and temporally uncorrelated jamming is taken into account, improving and extending earlier work on the same problem. [9]

• **ICA for Astronomical data**

ICA for removing artefacts from astronomical telescope images. To use ICA for the artefact detection and removal. This is motivated by the fact that for astrophysical data, the independence of the artefacts is often theoretically guaranteed, and also the linear mixing model holds exactly. This is an almost ideal application for ICA. In the astrophysical data, we have a number of digital images, recorded over consequent nights when the conditions are favourable, and carefully calibrated for geometrical and photometric alignments. ICA is then used for this image set to reveal independent components that might be artefacts. [9]

• **Electroencephalogram**

Electroencephalogram (EEG) is the recording of electrical activity along the scalp. An EEG data forms by recordings electrical potential of various points on the scalp. These potentials are presumably generated by some underlying components of brain activity [1]. This phenomenon is somewhat similar to as cocktail party problem. It is expected that only original components of brain activity should be recorded, but observation contains mixtures of components. ICA gives important information about the independent components of brain activity by giving access to it.

• **ICA for Feature extraction**

In the feature extraction the columns of mixing matrix A represents features and gives the coefficient of the th feature of an observed data vector x. Theory of redundancy reduction motivates to use ICA for feature extraction. [1]

• **Reducing Noise in Natural images**

An ICA algorithm finds wide application for removing noise from the images. This feature if ICA widely known as image denoising i.e. removal of white gaussian noise from the natural images.
X. SHORTCOMINGS OF ICA

- We cannot determine the variances (energies) of the independent components.
- We cannot determine the order of the independent components. The reason is that, again both s and A being unknown, we can freely change the order of the terms in the sum in, and call any of the independent components the first one.
- ICA assumes a linear stationary mixing model (the mixing matrix is a set of constants independent of the changing structure of the data over time). However, for many applications this is only true from certain observation points or for very short lengths of time. For example, consider the earlier case of noise on the ECG. [4]
- The sources mixed by A are assumed statistically independent. That is, they are generated from some underlying processes that are unrelated. In the cocktail party problem, this is trivially obvious; each speaker is not modulating their words as a function of any other words being spoken at the same time. However, in the case of the ECG noise/artefact removal, this is sometimes not true.[4]

XI. CONCLUSION

In this paper we have given the theoretical concept of Independent Component Analysis. We have discussed the basic definition of ICA along with its various models, and principle on which ICA works.

Then we have explained the concept of scatter plot which is basically used to proof the second principle i.e. presence of correlation between two variables or signals. And at last the various areas of areas are discussed in which ICA is widely used like that in image denoising, feature extraction, face recognition, Telecommunication and many more.

REFERENCES


